

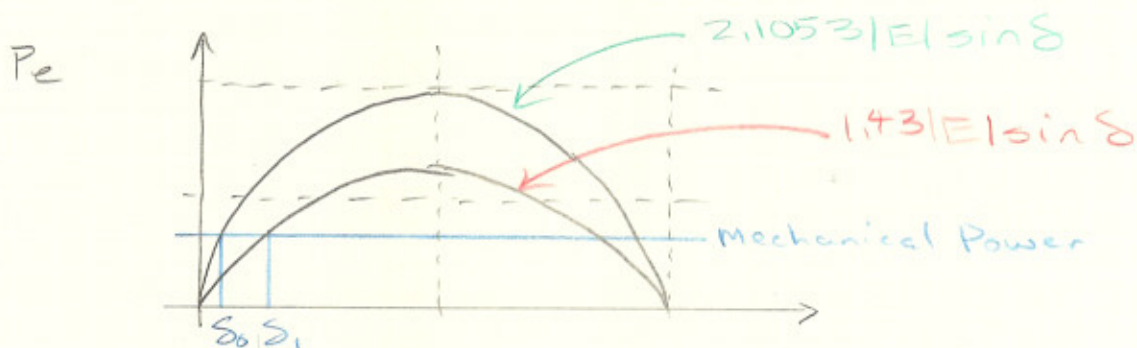
continued from last day...

P_e is the power received by the ∞ bus, changes in network configuration between sending end and receiving end, will change the value of X , hence the value of P_e .

For example, if one of the two parallel lines in the above network is removed, then the new X is equal to...

$$X = 0.7 \text{ PU}$$

$$P_e = \frac{|E|(1) \sin \delta}{0.7} = 1.43 |E| \sin \delta$$



The system delivers an apparent power of 1.1 p.u. at 0.85 PF lagging to two lines in service to an ∞ bus as shown above. Determine the source (excitation voltage) E and angle δ_0 under these conditions with the second line open, the new equilibrium angle δ_1 is reached. Find the electric power that can be transferred immediately following the cct opening as well as δ_1 . Assume that the excitation voltage E remains unchanged.

SOL:

$$\text{Power delivered} = P_e = 1.1 * 0.85$$

$$\text{Let } P_0 = P_e = 0.94 \text{ p.u.}$$

For the current \bar{I} in the circuit, we can write,

$$\bar{S}_0 = \bar{V}_\infty \bar{I}^*$$

$$\bar{I} = \frac{\bar{S}^*}{\bar{V}_\infty^*} = \frac{1.1(0.85 - j0.53)}{1.0 \angle 0^\circ} = 1.1 \angle -31.8^\circ$$

$$\bar{E} = |\bar{E}| \angle 0^\circ$$

$$\bar{E} \angle \delta = |\bar{V}|_\infty \angle 0^\circ + j \bar{I} X$$

$$jX = j0.15 + j0.1 + j0.45 // j0.45 = j0.475$$

then

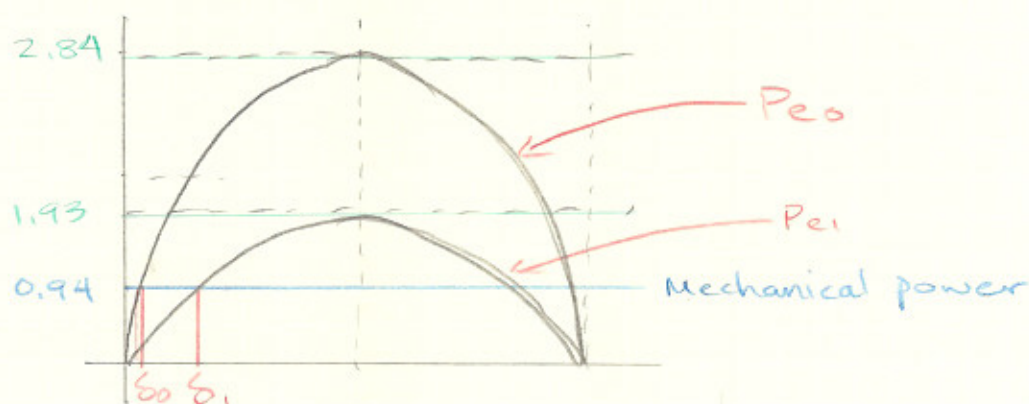
$$\begin{aligned} |\bar{E}| \angle \delta &= 1 + 0j + (1.1 \angle -31.8^\circ)(0.475 \angle 90^\circ) \\ &= 1.35 \angle 19.20^\circ \end{aligned}$$

With both lines in use, then the system is stable at $\delta_0 \dots$

$$\underline{\underline{\delta_0 = 19.20^\circ}}$$

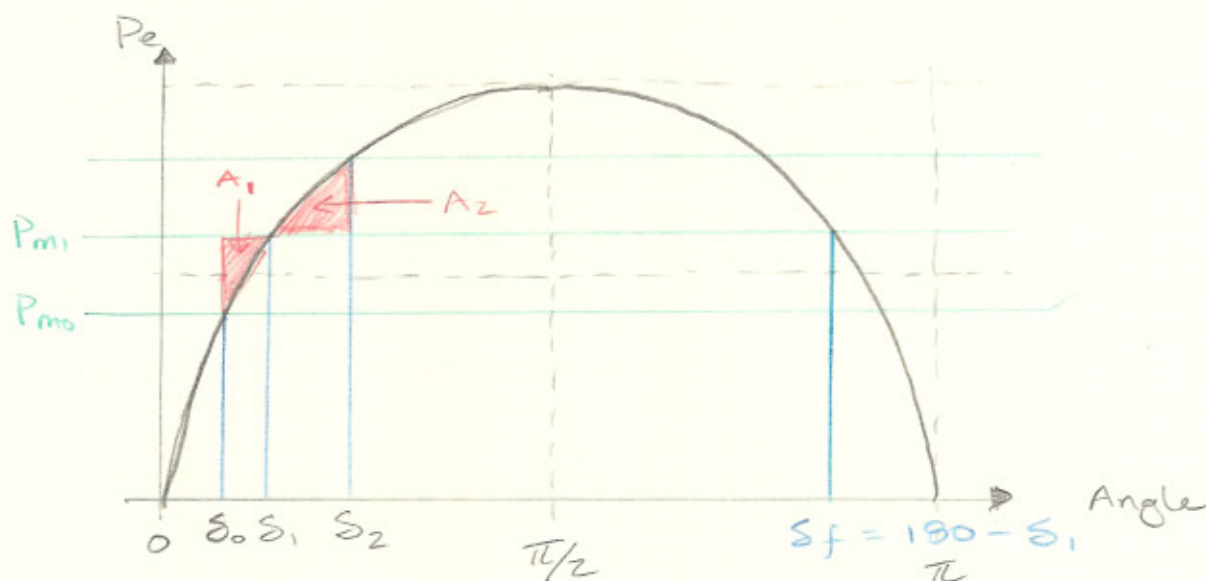
with one of the lines out of service, the new power $P_e = P_{e1}$ is:

$$\begin{aligned} P_{e1} &= (1.43)(1.35) \sin \delta \\ &= 1.93 \sin \delta \end{aligned}$$



S_1 can be found from $0.94 = 1.93 \sin S$.

EQUAL AREA METHOD



when $P_e = P_0$, then $P_e = P_{max} \sin S = P_0$, i.e. $P_{e1} = P_e$

If shaft power is increased to $P_{m1} = P_1$, then $P_1 - P_0 = P_1 - P_e = P_a$, where P_a is accelerating power, P_a will accelerate the rotor

P_a will accelerate the rotor and the additional energy will be stored in the inertia of the rotor, this will continue until S reaches and passes S_1

As S becomes greater than P_1 and the rotor decelerates so that the additional electric energy needed is supplied by the stored energy. Then S increases up to S_2 and starts decreasing, oscillating around S_1 until it reaches a new equilibrium state.

The excess energy stored in the inertia during the acceleration of the rotor is A_1 and is returned during the deceleration as A_2 . For net energy to be zero, then A_1 must equal A_2 , hence the equal area method.